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## The Crystal Structure of Ferrocarpholite

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Ferrocarpholite, the ferrous iron analogue of carpholite proper, is found to be an 'inosilicate' with  $(SiO_3)_n$ -chains very similar to those found in the pyroxenes. Its idealized formula is properly written  $FeAl_2(OH)_4Si_2O_6$ ; that of ordinary carpholite is  $MnAl_2(OH)_4Si_2O_6$ . The classification of carpholite, first given by Strunz, is therefore confirmed.

#### Introduction

Ferrocarpholite was described as a new mineral by De Roever (1951), who isolated it from rocks collected during the Celebes expedition 1929 of the Netherlands Geological Survey, under the leadership of Prof. H. A. Brouwer. Rotation diagrams of ferrocarpholite and carpholite proper from Wippra showed that the two are isomorphous (De Roever, 1951).

The extremely fibrous character of carpholite, and the length of its fibre period, 5.3 Å, led Strunz (1938) to suppose that carpholite has a chain structure related to that of the pyroxenes, and that its formula should be written  $(Mn, Fe)Al_2(OH)_4Si_2O_6$ , a classification which has since been accepted in most mineralogy handbooks. The proof, of course, is not conclusive as it stands. Moreover, since the pyroxenes themselves do not contain OH groups it was thought worth while to make a full structure determination.

## Properties of the specimen

The chemical composition has been given in De Roever's paper, to which we refer also for morphology, optics, etc. Whereas carpholite has been described by Strunz (1938) as monoclinic, ferrocarpholite is orthorhombic dipyramidal, the crystal class following unambiguously from the space group Ccca.

Cell constants were roughly determined from Weissenberg diagrams about the three axes; they were refined from rotation and oscillation diagrams about the c and b axes in a camera of 5.00 cm. radius, taken with Cu  $K\alpha$  radiation, the films being in the asymmetric position.

The cell dimensions thus determined,

$$a = 13.77, b = 20.18, c = 5.10$$
 Å,

have already been communicated in De Roever's paper; they are believed to be accurate within 0.1%.

Number of atoms per cellSi $16 \cdot 27$  $8 \times 2 \cdot 03$ Al $14 \cdot 99$ FeIII $0 \cdot 68$ T: $0 \cdot 07$ 

Al		( 14·99		
$Fe^{III}$		0.68	15 01	0, 1, 0,0
$\mathbf{Ti}$		0.07	19.91	9 X 1.99
Ma	1.69	∫ 0·07 J		
мg	1.03	<b>1</b> 1.56 ]		
Mn		0.05	8.12	$8 \times 1.01$
$Fe^{II}$		6.51		
$\mathbf{H}$		29·09 <sup>^</sup>		$8 \times 3.64$
0		78.92		$8 \times 9.87$

All halvings consistent with the space group Ccca are strictly observed. From the density,  $3.04 \text{ g.cm.}^{-3}$ ,

and the result of chemical analysis, De Roever cal-

culated the atomic contents of the unit cell as follows:

He gives reasons for the supposition that the water content, as determined by loss of weight after prolonged heating, is actually higher than given above; it seems therefore plausible to work with an idealized formula:

$$(F_{0.8}^{11}Mg_{0.2})(Al_{0.95}Fe_{0.05}^{111})_2Si_2O_{10}H_4$$
.

#### Determination of the structure

We shall describe our structure determination in some detail, first, because the economical use of Patterson and Fourier methods may be of some interest; secondly, because at one stage some use was made of the minimum-function method (Buerger, 1951), which has not yet been often applied in cases of such complexity, where no heavy atom is present.

As a first step, a projection of the vector map along [001] was calculated. Although it showed some indications of the presence of  $(SiO_3)_{\infty}$  chains of the same type as in the pyroxenes, we were not able to solve the structure from this map. In particular, it proved to be impossible to derive the Fe positions with any certainty; in this compound, Fe is not heavy enough to assign the highest peaks in the Patterson maps to Fe-Fe distances.

Three-dimensional data were then collected from Weissenberg photographs about the c axis (0 to 3rd layer), a axis (0 to 11th layer) and the zero and first

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Fig. 1. Patterson sections at (a) w = 0, (b)  $w = \frac{1}{2}$ , (c)  $w = \frac{1}{2}$ . On the right-hand side the significant interatomic distances are indicated. Overlap of u, v, 0 and  $u, \frac{1}{2}-v, \frac{1}{2}$  gives the vectors between atoms at z = 0 and  $z = \frac{1}{2}$ ; overlap of  $u, v, \frac{1}{2}$  and  $u, \frac{1}{2}-v, \frac{1}{2}$  identifies vectors between atoms at  $z = \frac{1}{6}, \frac{1}{3}, \frac{3}{2}$  and  $\frac{1}{6}$ . In the regions A and B there are several Si-O distances overlapping. All the peaks not shown in the right-hand figures can also be interpreted in terms of the structure parameters.

layer about the b axis. Notwithstanding the strong secondary radiation, pictures were made with Cu K radiation; in order to obtain as much information as possible, some photographs were also made with Mo K radiation.

The intensities were estimated visually by two investigators. The data are of rather poor quality, the spots being often split and the background being fairly heavy. The c-axis pictures were taken from a crystal ground to a cylinder of 0.6 mm. diameter; the crystal used for the a-axis pictures was a platelet with dimensions  $0.2 \times 0.05 \times 0.2$  mm. along the three crystallographic axes respectively. In view of other sources of error mentioned above, it was considered that for the latter crystal a correction for absorption would be hardly worth while. As a check, the background of the a-axis zero layer line, where irregular absorption might be feared, was measured along five traverses at different  $\theta$ -values; it has been shown (MacGillavry & Vos. 1943) that in the case of background caused chiefly by fluorescence, the background gives a fairly

reliable measure for the transmission factor of the coherently scattered radiation (Bragg spots). As the background for the a-axis picture was found to be practically constant, absorption was neglected. For the c-axis crystal, the absorption correction for a cylindrical rod was applied.

When the data had been collected and corrected for Lorentz and polarization factors, it became apparent that they showed some peculiar relations not inherent in the space group. Apart from space group absences it was noted that

hk3 is absent or very weak for even h and k, hk6 is absent for odd h and k.

On the other hand, reciprocal-lattice planes with  $l = 3n \pm 1$  show no indication of pseudo face-centring.

Moreover, it was noted that reflexions hk5 show parallelism with the corresponding hk1; to a much lesser degree this is the case also for hk6 and hk0, and hk4 and hk2 respectively. These peculiarities are

explained if we assume that most of the atoms in general position have a z-coordinate near  $\frac{1}{4}$ , the positions then being:

 $(0, 0, 0; \frac{1}{2}, \frac{1}{2}, 0) +$  $x, y, \frac{1}{3}; \overline{x}, \overline{y}, \frac{1}{3}; \overline{x}, \frac{1}{2} - y, \frac{1}{6}; x, \frac{1}{2} - y, \frac{5}{6};$  $x, \bar{y}, \frac{2}{3}; \bar{x}, y, \frac{2}{3}; \bar{x}, \frac{1}{2} + y, \frac{5}{8}; x, \frac{1}{2} + y, \frac{1}{4}.$ 

If all the atoms have these z values, it is easily shown that two Patterson sections only, i.e. those at w = 0 and  $w = \frac{1}{2}$ , would contain all the information\*. (This cannot be the case, however, since then  $I_{bkl}$ would be equal to  $I_{h,k,6-l}$ , and, as we saw, there is at most a tendency towards this regularity.) Patterson sections were made at w = 0,  $w = \frac{1}{2}$  and  $w = \frac{1}{3}$ (Fig. 1). The last two, which should be brought to coincidence by a shift  $0, \frac{1}{2}, \frac{1}{6}$  if all atoms were at  $z = \frac{1}{3}$  etc., showed, however, large differences. In fact, the highest peaks in the section  $w = \frac{1}{2}$  have no or insufficient coincidences in the plane  $w = \frac{1}{3}$ . On the other hand, it was found that to these high peaks  $u, v, \frac{1}{2}$  there correspond exactly peaks at  $u, \frac{1}{2} - v, 0$ (see Fig. 1(a) and (b)). This points to atoms at z = 0, as can be seen from inspection of the vector sets in the space group Ccca. A peak  $0, \frac{1}{4}, 0$ , which had about the expected height compared to the origin peak, was tentatively ascribed to Fe-Fe; Fe<sup>II</sup> would then be in the position (8b): 0, y, 0, etc., with  $y = 45^{\circ}$ . In order to find atoms in the plane  $z = \frac{1}{3}$ , the minimum function corresponding to this Fe–Fe peak at  $0, \frac{1}{4}, 0, \frac{1}$ was evaluated in the plane  $u, v, \frac{1}{3}$  (Fig. 2). This gave



Fig. 2. Minimum function  $u, v, \frac{1}{2}$ , corresponding to the shift 0, 1, 0 (Fe-Fe) and the shift 0, 1, 1 (Si-Si).

the position of three atoms which, from height, mutual distance and bond directions, could be easily identified as Si and two oxygens attached to it, as indicated in Fig. 2. There are some spurious peaks which could afterwards be interpreted as due to overlap: although the peak  $0, \frac{1}{4}, 0$  is single, the minimum function coincides in the plane  $u, v, \frac{1}{3}$  with the minimum function corresponding to a Si-Si peak  $0, \frac{1}{4}, \frac{2}{3}$ .

Comparison of the sections u, v, 0 and  $u, v, \frac{1}{2}$  revealed that the strong peaks in these sections could be explained if Al was assumed to be in two special positions, namely Al<sub>I</sub> in (8a) x, 0, 0, etc., with  $x = 69^{\circ}$ , and Al<sub>II</sub> in (8b) 0,  $y, \frac{1}{2}$  with  $y = 77^{\circ}$ . The rest of the

\* To avoid confusion, coordinates in vector space are indicated by u, v, w, coordinates in crystal space by x, y, z.

O atoms were then located from chemical considerations, with checks from the Patterson sections. Table 1 lists the rough atomic parameters.

Table	1.	Atomic	parameters	derived	from	Patterson
		section	s and minin	num fun	ction	

	<i>x</i> (°)	<i>y</i> (°)	z (°)
Fe	0	45	0
$Al_I$	69	0	0
$Al_{II}$	0	77	180
Si	69	47	240
OI	35	20	60
OII	70	20	240
OIII	90	60	330
OIV	30	55	240
Ov	30	75	60

The peculiarities in intensity distribution, mentioned above, are readily explained on the basis of the positions in Table 1: Fe and both sets of Al have face-centred configurations. Moreover, their contribution to the structure factor is a function of h, k, l (mod. 2). All atoms at  $z = \pm \frac{1}{2}$  or  $\pm \frac{1}{2}$  do not contribute to hk3 and hk6 with mixed indices: they have the same geometrical structure factor for hkl and h, k, 6-l. On the other hand,  $O_{\rm III}$ , the only set that does not conform to either of these rules, does not contribute to reflexions with odd l, as it is lying on the glide plane  $c(100)_{\frac{1}{4}}$ , so that the rule  $I_{hkl} = I_{h,k,6-l}$  is strictly valid only where O<sub>III</sub> atoms do not contribute, that is, for l = 1.

#### Refinement

Structure factors calculated with the positions of Table 1 showed already a remarkably good fit. The structure was refined by two-dimensional Fourier syntheses of the projections along [001] and [100], and subsequently by computing the three-dimensional series:

- (a) along x, 0, 0, for position of Al<sub>1</sub>;
- (b) along 0, y, 0, for Fe and Al<sub>II</sub>;
- (c) in the plane  $x, y, \frac{1}{6}$ , for Si, O<sub>I</sub>, O<sub>II</sub>, O<sub>IV</sub>, and O<sub>V</sub>; (d) in the plane  $x, y, -\frac{1}{12}$ , at x = 84, 90, and  $96^{\circ}$ , for  $O_{III}$ ;
- (e) along  $x = 70^{\circ}$ ,  $y = 46.8^{\circ}$ , z, for z value of Si.

The z parameters of the oxygen atoms I, II, IV and V were derived from the electron-density map projected along [100]. Although this projection shows

Tabl	e 2.	Final	atomic	parameters	of	ferrocary	ohol	it	e
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	<i>x</i> (°)	y (°)	z (°)
Fe	0	45.0	0
$Al_{I}$	68.3	0	0
$Al_{II}$	0	75.8	180
Si	70.0	46.8	237
0 <sub>I</sub>	35.0	20.2	<b>58</b>
$O_{II}$	<b>74</b> ·0	16.9	238
$0_{III}$	90.0	58.7	328
$\nabla_1 O$	29.4	$54 \cdot 3$	238
Οv	24.7	78.3	58

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much overlap, it was clear that all these z parameters are closely similar, and close to  $60^{\circ}$ .

After one cycle, the parameters were as given in Table 2.

As a final check, hk0 structure factors were calculated; the corresponding  $F_o$  were then scaled and the  $F_c$  corrected for temperature factor. The discrepancy factor R was then found to be 0.14, B being taken as 0.45 Å<sup>2</sup>. In view of the uncertainties in the experimental intensities (see above) it was not considered worth while to refine the structure further by difference syntheses.

### Discussion of the structure

Ferrocarpholite is a silicate of the  $SiO_3$ -chain type. In Fig. 3, which shows the structure viewed along the



Fig. 3. Structure of ferrocarpholite. The z values range from  $-\frac{1}{3}$  (lightest contours) to  $\frac{7}{12}$  (heaviest contours).

c axis, the part enclosed by broken lines is practically identical with part of the pyroxene structures. In the b direction the  $SiO_3$  chains are linked face to face by zigzag chains of Al in octahedral oxygen surroundings. A novel feature is that the same octahedral arrangement, with chain direction again parallel to the c axis, but with 90° difference in azimuth around this axis, occurs around Al<sub>II</sub>. In fact, the near surroundings of Al<sub>I</sub> and Al<sub>II</sub> are practically identical. This octahedral stacking is extended on both sides by octahedra around Fe, which follow closely the pattern around Al<sub>II</sub>. These broader ribbons of octahedra connect the  $Si_4Al_2O_{16}$  chains mentioned before.

Electrostatic valencies are practically balanced if it is assumed that  $O_{I}$  and  $O_{V}$  are OH groups.

Interatomic distances are not very accurate, for the reasons mentioned. However, it was found that Fe–O, Si–O and Al–O distances have the expected values: Fe–O = 2·16 Å (average of three, largest deviation from average 0·09 Å); Si–O = 1·64 Å (average of four, largest deviation 0·04 Å); Al<sub>I</sub>–O = 1·93 Å, average of three, largest deviation 0·05 Å); Al<sub>II</sub>–O = 1·92 Å (the average of three, largest deviation 0·07 Å); Si–O<sub>III</sub>–Si = 132°.

O-O distances within the tetrahedra vary between 2.55 and 2.74 Å, within Al octahedra from 2.50 to 2.96 Å. O-O distances within Fe octahedra, not belonging to Al coordination, vary from 3.16 to 3.24 Å.

Large O–O distances (3.51 Å) occur around the twofold axes parallel to the c axis (Fig. 3) for both  $O_{I}$ – $O_{I}$  and  $O_{III}$ – $O_{III}$ . These atoms do not belong to a common anion polyhedron. As  $O_{III}$  carries no hydrogen either, this distance seems to be a pure van der Waals distance, which gives 1.76 Å for the van der Waals radius of oxygen. Since both distances are independent of the z coordinates, they have a high accuracy.

No hydrogen bridges appear to be formed.

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